

### Reviews in Operator Theory 1980-86 Introduction by Paul R. Halmos

Operator theory is the branch of mathematics that treats the objects of analysis (numerical valued functions and their limiting properties) by the methods of modern topology and algebra. While, roughly speaking, the area 46 deals primarily with the objects (i.e., topological vector spaces) associated with the category of topological linear algebra, the area 47 deals with the morphisms between these objects (i.e., the mappings-both linear and nonlinear-between these spaces). Although functional analysis and operator theory developed as identifiable fields in the early part of this century they have seen tremendous growth in the past few decades and have found applications'to diverse areas, both to purely mathematical areas and to other scientific disciplines. These volumes contain a wealth of information about linear operators, algebraic systems of linear operators, differential and integral operators, and nonlinear operators.

All the *Mathematical Reviews* entries having operator theory (*MR* classification number 47) as a primary or secondary classification between 1980 and 1986 appear in these volumes. Within each section, reviews are ordered by their *MR* number. Relevant crossreferences are given with each review, and author and key indexes appear in the fourth volume.

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The papers published here relate to three different aspects of the conference. The first concerns topics relevant to all three fields, including, for example, Horn logic, lambda calculus, normal form reductions, algebraic theories, and categorical models for computability theory. In the area of logic, topics include semantical approaches to proof-theoretical questions, internal properties of specific objects in (pre-) topoi and their representations, and categorical sharpening of model theoretic notions. Finally, in the area of computer science, the use of category theory in formalizing aspects of computer programming and program design is discussed.

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Naomi Fisher, Harvey Keynes, and Philip Wagreich, Editors

(CBMS Issues in Mathematics Education, Volume 1)

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